

Resource Slope

Calculating slope

In a linear relationship containing the points (x_1, y_1) and (x_2, y_2) , slope can be computed using the formula:

$$\text{slope} = m = \frac{y_2 - y_1}{x_2 - x_1}$$

Keep in mind:

- Slope can be computed using any two points on a line. The points might be given in a problem description, presented in a table, or read from a graph of the line.
- The “y” values are always the dependent values in the problem, even if you choose a different variable to represent them.
- The “x” values are always the independent values in the problem, even if you choose a different variable to represent them.

If you need to review how to use the slope formula, you can view examples in the following video:

- http://www.youtube.com/watch?v=2kMUk_XRvRQ

The points in each of the following examples are presented in different ways. Review the example, then try your own.

1) Use two points to compute slope.

Example 1: Calculate the slope of the line between the points $(3, -2)$ and $(4, 7)$.

$$\text{slope} = m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{7 - (-2)}{4 - 3} = \frac{9}{1} = 9$$

You try: Calculate the slope of the line between the points $(-3, 5)$ and $(4, 16)$.

2) Use values in a table to compute slope.

Example 2: Calculate the slope of the line going through the points shown in the table and interpret the result.

| | | | | |
|----------------------|----|----|-----|-----|
| Time (sec) | 5 | 10 | 15 | 20 |
| Distance (yd) | 40 | 75 | 110 | 145 |

Choose any two points. For this example, we chose (5,40) and (15,110). The computation is as follows:

$$\text{slope} = m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{110 \text{ yd} - 40 \text{ yd}}{15 \text{ sec} - 5 \text{ sec}} = \frac{70 \text{ yd}}{10 \text{ sec}} = \frac{7 \text{ yd}}{1 \text{ sec}}$$

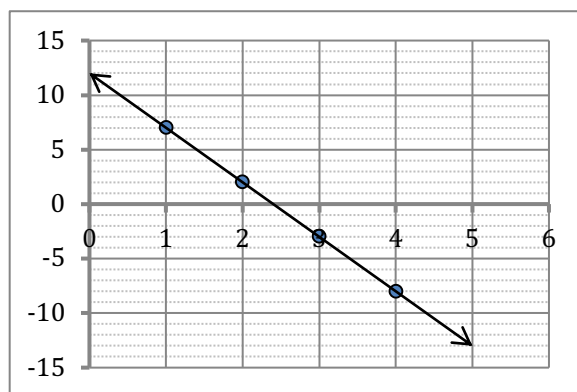
We interpret the slope using this statement: "The distance changes seven yards every one second."

You try: Calculate the slope of the line going through the points shown in the table and interpret the result.

| | | | | |
|------------------|----|----|----|----|
| Snacks | 5 | 10 | 15 | 20 |
| Cost (\$) | 15 | 30 | 45 | 60 |

3) Use values from a graph to calculate slope.

Example 3: Calculate the slope of the line shown in the graph.



Choose any two points from the graph. For this example, we chose (2,2) and (3,−3). The computation is as follows:

$$\text{slope} = m = \frac{y_2 - y_1}{x_2 - x_1}$$

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$$m = \frac{-3 - 2}{3 - 2} = \frac{-5}{1} = \frac{-5}{1} = -5$$

You try: Calculate the slope of the line shown in the graph.

